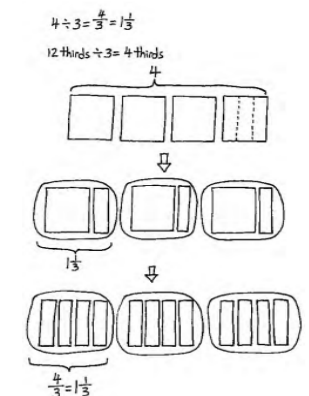


## Multiplication and Division of Fractions and Decimal Fractions

In this 38-day module, students learn to multiply fractions and decimal fractions and start work with fraction division. Students will begin by measuring fractional parts on a number line as a concrete way of understanding fractional parts of a whole, and eventually move to more abstract fraction operations.

A diagram of  $4 \div 3$  showing fractional division:



**New Terms in this Module:**  
 Decimal divisor- the number that divides the whole and that has units of tenths, hundredths, thousandths, e.g.  $1/100$

**Simplify-** using the largest fractional unit possible to express an equivalent fraction, e.g.  $4/6$  simplifies to  $2/3$ , with the denominator 3 being a larger fractional unit than 6

**Familiar Terms with some definitions:**

**Denominator**  
**Decimal Fraction**  
**Equation**  
**Equivalent Fraction**  
**Factors** - numbers that are multiplied to obtain a product  
**Line Plot**  
**Mixed Number**  
**Numerator**  
**Tape Diagram**  
**Unit** - one segment of a partitioned tape diagram  
**Unknown** - the missing factor or quantity in multiplication or division  
**Whole Unit** - any unit that is partitioned into smaller, equally sized fractional units

$4 \div 3$ , shown as a traditional algorithm division problem:

$$\begin{array}{r} 1\frac{1}{3} \\ 3 \overline{)4} \\ \underline{-3} \\ 1 \end{array}$$

check:  $3 \times 1\frac{1}{3}$   
 $= 1\frac{1}{3} + 1\frac{1}{3} + 1\frac{1}{3}$   
 $= 3 + \frac{3}{3}$   
 $= 4$

Each bag of cats weighs  $1\frac{1}{3}$  Kilograms.

**What Came Before this Module:** We learned to add and subtract fractions with unlike denominators, moving from concrete to abstract examples.

**What Comes After this Module:** In Module 5, we will work with the area and volume of two- and three-dimensional figures.

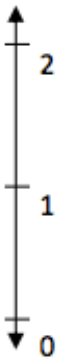
## + How you can help at home:

- Continue to practice and review multiplication and division math facts - this greatly supports work with fractions!
- Look for opportunities in daily life to discuss both fractional parts of a whole and of other fractions, e.g. What is  $\frac{1}{4}$  of 20?  $\frac{1}{4}$  of  $\frac{1}{2}$ ?

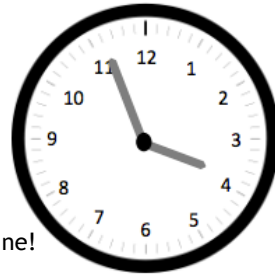
## Key Common Core Standards:

- Write and interpret numerical expressions.
- Perform operations with multi-digit whole numbers and with decimals to hundredths.
- Apply and extend previous understandings of multiplication and division to multiply and divide fractions.
- Convert like measurement units within a given measurement system.
- Represent and interpret data.

Various types of number lines:



Vertical number line



The clock - a circular number line!

A ruler number line



Spotlight on Math Models:

## Number Lines

You will often see this mathematical representation in *A Story of Units*.

*A Story of Units* has several key mathematical “models” that will be used throughout a student’s elementary years.

The number line is a powerful, flexible model that students can use in many ways. In this particular module, students begin to understand the idea of fractions as division by marking a ruler or line plot with  $\frac{1}{2}$ ,  $\frac{1}{4}$ , and  $\frac{1}{8}$  increments.

The number line is used beginning in Kindergarten in *A Story of Units*, and will continue to appear in various forms through 5<sup>th</sup> grades. It is used to develop a deeper understanding of whole number units, fraction units, measurement units, decimals, and negative numbers. Often, the mathematical concepts in an *ASOU* module move from concrete to more abstract, and the number line is an important concrete conceptual step for students of all ages.

Sample Problem from Module 4:  
(Example taken from Lesson 5)

Forty students shared 5 pizzas equally. How much pizza did each student receive?

What fraction of the pizza did each student receive?

Note the use of a tape diagram as well as the drawing showing division of a whole number into fractional parts:

